Gilbert damping tensor within the breathing Fermi surface model: anisotropy and non-locality

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Abstract

In magnetization dynamics, the Gilbert damping $\alpha$ is often taken as a parameter. We report on a theoretical investigation of $\alpha$, taking into account crystal symmetries, spin–orbit coupling and thermal reservoirs. The tensor $\alpha$ is calculated within the Kamberský breathing Fermi-surface model. The computations are performed within a tight-binding electronic structure approach for the bulk and semi-infinite systems. Slater–Koster parameters are obtained by fitting the electronic structure to first-principles results obtained within the multiple-scattering theory. We address the damping tensor for the bulk and surfaces of the transition metals Fe and Co. The role of various contributions are investigated: intra- and interband transitions, electron and magnetic temperature as well as surface orientation. Our results reveal a complicated non-local, anisotropic damping that depends on all three thermal reservoirs.

1. Introduction

Magnetic devices and magnetic reversal effects are strongly affected by their rate of energy transfer (dissipation): the larger this transfer, the faster the magnetic equilibration. Regarding spintronics applications, there is an ongoing search for materials with preferably small damping \cite{1}. The magnetization dynamics on a nanometer length scale and on a femtosecond...
time scale can be described by the Landau–Lifshitz–Gilbert (LLG) equation [2]. Here, the dissipation is introduced by Gilbert's phenomenological parameter $\alpha$ [3] that includes all possible damping mechanisms. The damping parameter is taken as local and isotropic, in agreement with ferromagnetic resonance spectroscopy [4, 5].

The coupling of the magnetization to the electronic degrees of freedom is mediated by spin–orbit coupling. Detailed measurements on the atomic scale as well as theoretical models for nanostructures reveal a non-uniform spin–orbit coupling [6] which is responsible for local magnetic anisotropies. Hence, the Gilbert damping should also be anisotropic and site-dependent, in particular in low-dimensional systems.

To calculate the damping constant from first principles, Ebert et al [7] suggest a model that shows a good agreement with experiments. Based on the linear response theory, their torque–torque correlation model was applied to an Fe$_{1-x}$Co$_x$ alloy and to various 5d transition metals. Thermal effects are included by phonon scattering in an alloy-analogy model.

Besides linear response theory, there exists also the breathing Fermi surface model of Kamberský [8, 9]. This model considers the non-equilibrium population of electronic states that is forced by the change of the magnetic moments. The coupling of the electronic spin to the electronic eigenstates is of spin–orbit nature. The model predicts a significant damping in metals with strong spin–orbit coupling, e.g. 4f metals. Also ultrathin films are predicted to exhibit strong damping [10].

The energy change near the Fermi surface of the Stoner magnets Fe and Co has been investigated by Gilmore et al [11], using the Kamberský model in a projector augmented wave method. Although in good agreement with experimental findings, their results do not comply with those by Fähnle and Steiauf [12] where a dependence of the damping $\alpha$ on the magnetic moment's direction [13] as well as on temperature is established. The latter has been observed experimentally [14–16] and confirmed theoretically [7, 10]. The Gilbert damping for (oxidic) nanoparticles [17], Ni–Fe and Ni–Co alloys [18], half metals [1], Co/Ni multilayers [19] and magnetic thin films [20–22] were also studied recently. Such materials are recommended for spintronic applications due to their high spin–orbit coupling and, thus, enhanced Gilbert damping. Furthermore, the damping can become anisotropic and non-local [23–25], leading to a damping tensor $\alpha_{ij}$. The anisotropic and non-local character of the magnetic damping is also achievable within the Kamberský model.

In this paper we report on a theoretical investigation of the anisotropic and non-local Gilbert damping in the framework of the Kamberský model. To calculate the damping tensor, we use a tight-binding (TB) model. The TB parameters have been obtained by fitting the electronic structures to those of a first-principles fully relativistic multiple scattering Korringa–Kohn–Rostoker (KKR) method using a genetic algorithm. Semi-infinite systems are treated by a renormalization scheme for the Green function. These together with the generalized Kamberský equation allow calculation of the layer- as well as the temperature-resolved damping tensor. We compare our results to published data for Fe and Co. The role of various contributions are analyzed in detail: electronic intra- and interband transitions, electron and magnetic temperature as well as surface orientation. Our results reveal a complicated non-local, anisotropic damping that depends on all three thermal reservoirs.

The paper is organized as follows. Computational details and theoretical basics are given in section 2. The damping properties of bulk magnets are discussed in section 3.1, for surfaces in section 3.2.
2. Theoretical and computational aspects

We consider a ferromagnetic system whose Bloch states, characterized by the band index \( n \) at wavevector \( k \), have energies \( \varepsilon_{k,n} \). Due to the spin–orbit coupling, the magnetization \( m \) with direction \( e \) affects the eigenstates: tilting \( m \) by a small change \( \delta e \) generates a non-equilibrium population state which can be viewed as a deviation—or breathing—of the Fermi surface. The non-equilibrium distribution relaxes toward the equilibrium distribution within a time \( \tau_{k,n} \) (relaxation time approximation). This relaxation is driven by the coupling \( \Lambda \) of the electron reservoir to the lattice reservoir, that is via the electron–phonon coupling. Following Gilmore et al. [11], this breathing Fermi surface model of Kamberský [8, 9] in a generalized form and within the isotropic relaxation time approximation (\( \tau_{k,n} \rightarrow \tau \)) results in the damping tensor \( \alpha \) with elements

\[
\alpha^{\nu\mu} = \frac{g\pi}{m} \sum_{n,m} \int \eta(\varepsilon_{k,n}) \left( \frac{\partial \varepsilon_{k,n}}{\partial \delta e} \right)_v \left( \frac{\partial \varepsilon_{k,m}}{\partial \delta e} \right)_\mu \frac{\tau}{\hbar} \frac{dk}{(2\pi)^3} \quad \nu, \mu = x, y, z,
\]

\( \eta(\varepsilon_{k,n}) = \frac{\partial f(\varepsilon)}{\partial \varepsilon} \bigg|_{\varepsilon_{k,n}} \) is the derivative of the Fermi–Dirac distribution \( f(\varepsilon) \) with respect to the energy; \( n \) and \( m \) are band indices.

The spin–orbit coupling \( \hat{H}_{so} \) correlates the magnetization with the electronic ground state, giving rise to the magnetocrystalline anisotropy. Hence, the torque matrix elements \( \frac{\partial^2 f(\varepsilon)}{\partial \varepsilon^2} \bigg|_{\varepsilon_{k,n}} \) can be obtained from \( f(\delta e) = \langle n, k | e^{i\sigma \cdot \delta e} \hat{H}_{so} (e) e^{-i\sigma \cdot \delta e} | m, k \rangle \), where \( | n, k \rangle \) are the eigenstates of the Hamiltonian \( \hat{H} \) and \( \sigma \) is the vector of Pauli matrices. With \( \Gamma_{nm} \equiv \langle n, k | [\sigma, \hat{H}_{so}] | m, k \rangle \), which accounts for the transitions between the states in bands \( n \) and \( m \), the damping tensor \( \alpha^{\nu\mu} \) reads

\[
\alpha^{\nu\mu} = \frac{g\pi}{m} \sum_{n,m} \int \Gamma^n_\nu \Gamma^m_\mu W_{nm}(k) \frac{dk}{(2\pi)^3}.
\]

The scattering events depend on the overlap \( W_{nm}(k) \equiv \int d\varepsilon \eta(\varepsilon) A^k_\Lambda(n)(\varepsilon) A^m_\Lambda(m)(\varepsilon) \) of the spectral function \( A^k_\Lambda(n) \), which is a Lorentzian centered at \( \varepsilon_{k,n} \). Its width is determined by the coupling strength \( \Lambda \) to the lattice. Replacing the Bloch states by the Green function, the spectral function can be written as \( \text{Im} \hat{G} (k, \varepsilon \pm i\Lambda) = \mp \sum_n \langle n | \Lambda | n \rangle A_\Lambda(\varepsilon - \varepsilon_{k,n}) \). Hence, we end up with a result similar to the torque–torque-correlation model [7],

\[
\alpha^{\nu\mu} = \frac{g}{m\pi} \int \int \eta(\varepsilon) \text{Tr} \left( \hat{T}^\nu \text{Im} \hat{G} \hat{T}^\mu \text{Im} \hat{G} \right) \frac{dk}{(2\pi)^3} d\varepsilon,
\]

where \( \hat{T} \equiv [\sigma, \hat{H}_{so}] \).

To obtain the Green function, we use a TB model [26] based on the Slater–Koster parameterization [27, 28]. The TB parameters, including the spin–orbit coupling strength, are obtained by fitting the TB band structures to \( ab \) initio band structures, using a genetic algorithm [29] (table 1). The fitness function is taken from [30], with an accuracy better than \( 10^{-4} \) eV. The parameters are in good agreement with those reported in [31–33]. The first-principles band structures were calculated within a fully relativistic multiple-scattering Green function approach (KKR method) [34].

Having a reliable TB description of the bulk electronic structure at hand, we proceed by computing the electronic structure of a semi-infinite system, using a renormalization
The effective field \( B_i = \frac{\partial \hat{H}_{\text{mag}}}{\partial m_i} \) is fixed by the Hamiltonian \( \hat{H}_{\text{mag}} \) which comprises the Heisenberg exchange interaction, the dipole–dipole energy, the magnetocrystalline anisotropy and a Zeemann term. Explicitly,

\[
\hat{H}_{\text{mag}} = - \sum_{ij} m_i \mathbf{A}_{ij} m_j - \sum_i \mathbf{B}_{\text{ext}} \cdot m_i.
\]
\[ I_{ij} = J_{ij} E + Q_{ij} \] for \( i \neq j \) contains the Heisenberg exchange parameter \( J_{ij} \) and the dipolar interaction matrix \( Q^{\nu\mu}_{ij} = \frac{1}{2\mu_0} \frac{3r_{ij}^3 - r_{ij}^6}{r_{ij}^7} \) between two sites \( i \) and \( j \) with distance \( r_{ij} = r_i - r_j \). \( E \) is the unit matrix. \( I_{ij} \) determines the magnetoelastic anisotropy. The Heisenberg exchange interactions \( J_{ij} \) as well as the anisotropies \( I_{ij} \) have been calculated from first principles within the KKR framework, using the Lichtenstein formula \[ [42] \) and the magnetic force theorem \[ [34] \); for details see \[ [43] \).

### 3. Results and discussion

#### 3.1. Damping constant of bulk materials

In this section, we first address the two approaches to \( \alpha \), (1) and (3), and compare our TB data to the ab initio results reported in \[ [11] \). We assume a ferromagnetically ordered system with magnetic moments in \( e_c \) direction. Tilting a magnetic moment toward \( e_x \) or \( e_y \) yields an effective torque matrix element \( T^- \equiv \langle n, k | \sigma^-, \hat{H}_{so} | m, k \rangle \), where \( \sigma^- \equiv \sigma^x - i \sigma^y \). The cubic symmetry in bulk bcc Fe and fcc Co dictates that the damping tensor is diagonal, in agreement with our calculations. The damping constant \( \alpha \) is then given by the trace of the damping tensor \( \alpha \) for the reference magnetization direction \( e_c \) \((\alpha = \alpha^{xx} + \alpha^{yy}) \) \[ [11] \).

The reliability of our TB parameterization is proven by the agreement of the damping constant \( \alpha \) with those reported in \[ [11] \) (figure 1). For comparison, the TB damping constants have to be scaled by a factor of \( 1/4\pi^2 \), which we attribute to a different definition of the Lorentzian in \[ [11] \).

For large electron–phonon coupling \( \Lambda \), \( \alpha \) decreases, which is interpreted as follows. \( \alpha \) comprises both intraband transitions \((n = m \) in (2); blue line in figure 1) and interband transitions \((n \neq m \); green line in figure 1) \[ [11] \). Energy levels \( n \) and \( m \) located close to each other accelerate the relaxation of the electron–hole pairs and, thus, decrease the Gilbert damping. The phonon reservoir ‘smears out’ the electron bands: the broadening of the electron spectral density is larger, the stronger electrons and phonons are coupled. Thus, the probability of transitions between states \( n \) and \( m \) is increased. For small \( \Lambda \), the intraband transitions play a major role, where \( \alpha^{\text{int}}(\Lambda) \) can be approximated linearly. For large \( \Lambda \), the broad Lorentzians overlap (cf figure 3(a)) and lead to an increase of the interband contribution which eventually dominates the intraband contribution. This allows hopping of the electrons between states \( n \) and \( m \). For even larger \( \Lambda \), the Gilbert damping drops again, resulting in the maximum at \( \Lambda \approx 1 \). However, this is an artifact of the finite orbital basis in the TB approach which does not describe well electronic states far off the Fermi level (at \( \approx 10 \) eV). Nevertheless, the approach reproduces the ab initio results of \[ [11] \) in the range \( \Lambda \in [0.001, 1] \) well.

In the ‘Lorentz’ approach (2), the coupling \( \Lambda \) defines the width of the energy window in which transitions \( \Gamma_{nm} \) are accounted for; the electronic structure itself is unaffected. In the Green function approach, \( \Lambda \) is taken as the imaginary part of the energy at which the Green functions is evaluated. This offset from the real energy axis provides a more accurate description with respect to the ab initio results \[ [11] \) than the Lorentzian approach, in particular for Fe. This may be understood from the fact that a finite \( \Lambda \) broadens and shifts maxima in the spectral function; hence, electronic states at energies around the Fermi level that are weakly weighted by \( \eta(\varepsilon) \) contribute to the damping. Furthermore, their contribution depends on their orbital composition and on the strength of the spin–orbit coupling.
We now discuss the dependence of $\alpha$ on the reservoir temperatures and focus first on the spin temperature $T_s$. The dependence of $\alpha$ on the magnetic moment direction $e$, on the electron–phonon coupling $\Lambda$ as well as on transitions involving energetically lower states suggests a correlation between the spin, lattice and electron temperature [44]. The spin temperature $T_s$ is modeled within the DLM theory [45, 46]. This approach is based on a substitutional binary alloy that is described within the CPA [39, 40, 47]; the host material comprises sites with magnetization along the reference direction $e$, with concentration $c_{\uparrow}$, and sites with magnetization along $-e$, with concentration $c_{\downarrow} = 1 - c_{\uparrow}$ [48] (figure 2). Zero spin temperature is obtained for $c_{\uparrow} = 1.0$ (ferromagnetic case), whereas the critical temperature is given for $c_{\uparrow} = 0.5$ (paramagnetic case). The mapping of the impurity concentration on the spin temperature can be obtained by comparing magnetizations derived from DLM electronic-structure calculations and from temperature-dependent Monte Carlo calculations [48, 49].
The dependence of $\alpha$ on the spin temperature (figure 2) is in agreement with the dissipation-fluctuation theorem which states, roughly speaking, that the dissipative reaction of the system is proportional to the fluctuation. Here, the electron system tries to stabilize the magnetic order with increasing $T_s$ (that is increasing magnetic fluctuations or decreasing concentration) by increasing the Gilbert damping which models the dissipation. The sizable change of $\alpha$ with concentration suggests that a constant $\alpha$ may be inappropriate for modeling magnetic systems at elevated temperatures, for example using the LLG equation.

We now turn to the dependence of $\alpha$ on the electron temperature $T_e$. The electron temperature is included via $\eta$ in (1) and accounts for transitions between states in a narrow energy window above the Fermi level. An electron–hole pair relaxes faster from the non-equilibrium population (which is induced by the spin–orbit coupling) toward the equilibrium than in the zero temperature case; thus, $\alpha$ decreases with decreasing relaxation time $\tau$. This mechanism is contrasted by the fact that more electronic states around the Fermi level are involved in the relaxation process, leading to an increase of $\alpha$. Hence, the Kamberský model postulates a competition between these two mechanisms (figure 3).

We limit the dependence of $\alpha$ on the electron temperature by the energy window around the Fermi level $\varepsilon_F$ to $\varepsilon_{cut} = 0.01, 0.1$ and $1.0$ eV (figure 3). For a large energy window of $\varepsilon_{cut} = 1$ eV, $\alpha$ increases non-linearly with electron temperature; a similar trend is found for the magnetic temperature $T_s$. This finding is explained by the large spectral overlap $W_{nm}$ (figure 3(a)): $W_{nm}$ is constrained by the derivative $\eta$ of the Fermi–Dirac distribution. The higher the temperature, the larger the spectral overlap (color shaded areas in figure 3(a)) and therefore, $\alpha$ increases. If $\varepsilon_{cut}$ is smaller than the underlying range of the Fermi–Dirac distribution, $\alpha$ decreases with the temperature.

\textbf{Figure 2.} Damping constant $\alpha$ versus spin temperature $T_s$ for bulk Co (triangles) and Fe (circles), as modeled by the concentration $c_{\parallel}$ in the DLM theory (see the text). The concentration is inversely proportional to the temperature [48]. Data for electron–phonon coupling $\Lambda = 0.1$ eV (0.01 eV) are displayed in blue (red). The electron temperature $T_e$ is zero. Lines serve as guides to the eye.
Figure 3. (a) Illustration of the spectral overlap contribution between electronic state \( i \) and \( j \) for temperatures \( T_1 < T_2 < T_3 \). With increasing temperature the relevant energy window around the Fermi energy \( E_F \) becomes larger, leading to an increased Gilbert damping \( \alpha \). (b) \( \alpha \) versus electron temperature \( T_e \) for a fixed electron–phonon coupling \( \Lambda = 0.1 \) for Co (triangles) and Fe (circles). Energy cut-offs are distinguished by colors: \( \varepsilon_{\text{cut}} = 0.01 \) eV green, 0.1 eV blue and 1.0 eV red. The spin temperature \( T_s \) is zero. Lines serve as guides to the eye.

The electron–phonon coupling is, at present, roughly modeled by a constant \( \Lambda \). Phonons can be included via the spatial dependence of the TB parameters, for example using Harrison’s law [28] or by a polynomial representation [50]. In particular the latter reproduces well phonon dispersions. The atomic displacements change the electronic structure around the Fermi level and remove degeneracies in the band structure; thus, the accompanying decrease of contributions from intraband transitions will reduce \( \alpha \) [7]. In addition, electron–magnon scattering or the Eliott–Yafet-type spin scattering mechanism could be included [51].

The damping tensor (1) motivated in [12, 13] accounts for transitions between states with different reference spin direction and, thus, also for spin–flip transitions. For cubic symmetry, the damping tensor is diagonal. In contrast to bulk systems, off-diagonal elements could be non-zero in systems with reduced symmetry, for example at surfaces.
3.2. Damping tensor at surfaces

In the following, we address the electronic contribution to the damping tensor $\alpha$ at surfaces. As examples, we focus on (001), (110) and (111) surfaces of fcc-Co with Cu lattice constant 3.54 Å, addressing thick Co films on Cu surfaces.

The Rayleigh dissipation functional predicts energy transfer between neighboring sites $I \neq J$ [52, 53]. Hence, the energy transfer rate has to be considered as a non-local, rather than as a local (on-site) quantity [3]. In contrast, on-site contributions account for a local coupling to the lattice reservoir (phonons). To simplify the discussion, we define a shell-averaged damping tensor $\alpha(r)$ by considering a reference site $i_0$ in layer $n_0$ ($I_0 = (n_0, i_0)$) and summing up contributions from all sites $j$ in layer $m$ ($m \neq n_0$ and $j \neq i_0$) that are located on a sphere with radius $r$ (figure 4).

For all three surfaces, the energy transfer is short-ranged, as is evident from the decrease of $\alpha$ with distance $r$ (figure 4). The damping depends also on the surface orientation: the nearest-neighbor $\alpha$’s differ slightly ($\alpha_{NN, I_0}^{(001)} = 0.023$, $\alpha_{NN, I_0}^{(110)} = 0.025$ and $\alpha_{NN, I_0}^{(111)} = 0.022$), as can be explained qualitatively by the coordination numbers of site $I_0$ (8, 7 and 9 for (001), (110) and (111), respectively). If only nearest-neighbor hopping would be considered, a reduced coordination yields a small electron hopping probability (small band width), resulting in both a minute energy transfer and damping constant.
\( \alpha \) decreases with layer index (inset in figure 4). The topmost layer shows the largest dissipation for all three surfaces, which is in accordance with the fluctuation-dissipation theorem. NB: in the LLG equation, the fluctuation amplitude (that is the width of the Gaussian distribution of the random magnetic field [2]) reads \( \alpha \cdot k_B T / \gamma m \); hence, the response at a temperature \( T \) is stronger at the surface than in the bulk. The dependence of \( \alpha \) on the layer index is non-monotonous and exhibits oscillations; this finding is at variance with results reported in [54] but agrees with those in [23, 24]. The oscillations can be explained by the density of states of the \( d \) states which ‘carry’ the magnetic moment of Co.

The density of states of \( d \) orbitals at the Fermi level is largest for the surface layer (figure 5). It oscillates similarly to \( \alpha \); this coincidence has been already noticed in [7, 55]. The oscillations are explained by the behavior of \( t_{2g} \) and \( e_g \) states: the density of states (DOS) \( n_{t_{2g}}(\varepsilon_F) \) decreases monotonically with layer index but \( n_{e_g}(\varepsilon_F) \) shows an oscillatory behavior.

Eventually, we address how the non-locality of the Gilbert damping \( \alpha_{ij} \) affects the magnetization dynamics in different layers, using (5) on a fs-time scale. The non-locality is relevant in an incoherent magnetic configuration, e.g. in demagnetization processes [55] or in nutation [56], both relevant on femtosecond or picosecond time scales; in case of a coherent precession of the magnetic moments, the sum in (5) can be replaced by an effective constant \( \alpha_{ij}^{\text{eff}} = \sum_j \alpha_{ij} \) [10]. We discuss its effect for the nutation in a two-layer thick Co film on Cu(111) [56]. Here, we include \( \alpha(r) \) from Co(111) up to third-nearest neighbors (\( r = 4.4 \text{ Å} \)) (figure 6). Here, the electron and spin temperature are zero; the electron–phonon coupling enters with \( \Lambda = 0.01 \text{ eV} \).

Assuming a linear temperature dependence of the electron–phonon coupling \( \Lambda = B T_{\text{ph}} \) (e.g. \( B = 0.011 \text{ eV K}^{-1} \) for nickel)—as in the Drude model [57]—a finite \( \Lambda \) requires a finite
Figure 6. Nutation of a surface magnetic moment in a two layer thick Co film on Cu(111) of (a) a coherent and (b) a non-coherent spin state. \( m_z \) is shown versus time for different damping scenarios: considering the non-local \( \alpha_{ij} \) (red); effective \( \alpha \) integrated over the distance \( r \) (green, 0.083 for the surface and 0.021 for the subsurface layer), and effective \( \alpha \) integrated over \( r \) and weighted by the coordination number (blue, 0.12 for the surface and 0.028 for the subsurface layer).

The phonon temperature \( T_{ph} \). Here, we choose a value of 1 K. In accordance with Ebert et al [7], this implies that the Kamberský model fails for zero phonon temperature because it results in an infinite Gilbert damping. Nevertheless, the chosen small \( T_{ph} \) allows the LLG equation to be applied for zero electron and spin temperatures.

An initial incoherent state is prepared by perturbing randomly the coherent precession around the anisotropy field at time \( t = 0 \). Then, an external magnetic field with a strength of \( B = 5 \) T is abruptly switched on. We study three cases: accounting for (i) the non-local \( \alpha_{ij} \); (ii) an effective \( \alpha \) by summing over the distances \( r \); and (iii) an effective \( \alpha \) by summing over distance \( r \) but weighted with the respective coordination numbers.

Both the nutation lifetime and the amplitude are reduced with higher damping, which supports the proportionality of the moment of inertia and the damping [58]. Case (ii) exhibits the smallest damping and, thus, a larger duration of the nutation. For case (i) the energy transfer to the neighboring sites accelerates the relaxation process compared to the other two cases. In contrast to the extended LLG equation used in [56], the present LLG equation (5) does not contain the magnetic moment of inertia and, thus, does not comprise a nutation term. Bhattacharjee et al [59] showed the existence of nutation without extension of the LLG equation. This finding is fully confirmed in our study by the increased nutation lifetime on a ps-time scale which differs from that in [56].

A coherent precession of all magnetic moments (figure 6(a)) gives a small phase shift (up to 10 fs), which is due to the direct coupling to the inert motion of site \( j \). In an incoherent state, the evolution of \( j \) appears as a superimposed ‘noisy signal’ (red in figure 6(b)). According to the angular-momentum transfer present in the Heisenberg model, the energy transfer depends to the coordination: the higher the coordination number, the faster the relaxation. We conclude that anisotropic dissipation is advantageous in relaxation and switching processes in magnetic nanostructures.
4. Conclusion

We present a calculational method to obtain the Gilbert damping tensor based on the breathing Fermi-surface model. Within a TB approach the layer-dependence of the damping has been obtained. The non-local dissipation rate depends mildly on the surface orientation but strongly on the layer and on the distance to neighboring sites. In the tensor representation, the correlation to the reference magnetization results in a non-homogeneous dissipation, which suggests to consider the dependence of the Gilbert damping on the direction of the magnetic moments in future magnetization dynamics simulations.

We also studied the dependence of the Gilbert damping constant on the electron and spin temperatures. The damping increases with temperature, in contrast to experimental observations; this finding supports the fact that the phonon temperature is the major thermal contribution. The present comparably simple approximation of the electron–phonon coupling has to be improved in a future implementation. Nevertheless, the spin as well as the electron temperature should be considered in incoherent magnetization effects.

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